

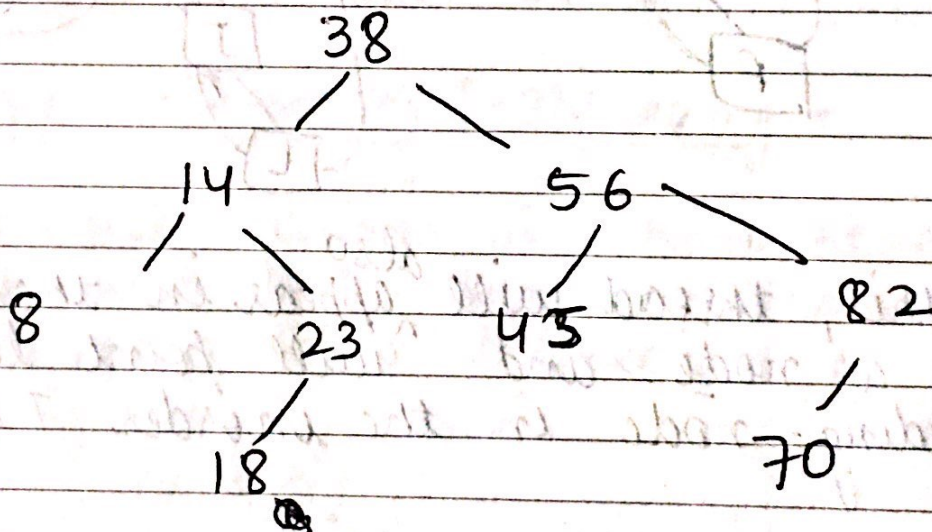
* BINARY SEARCH TREES

Suppose T is a binary tree.

Then T is called a binary search tree if each node N of T has the following property :-

The value at N is greater than every value in the left subtree of N and is less than every value in the right subtree of N .

eg



ITEM = 20 Inserted.

Insert 20 to the right of 18

eg 40, 60, 50, 33, 55, 11

THINGS TO DO

~~Create a numbers~~

Create Binary Search Tree

JUNE '13						
S	S	F	T	W	T	S
	1	2				
3	4	5	6	7	8	9
10	11	12	13	14	15	16

JULY						
M	T	W	T	F	S	S
1	2	3	4	5		
8	9	10	11	12		

MOTIVATIONS

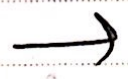


TEAMWORK

Talent wins games,
but Teamwork and
intelligence wins Champions.

MEMO

MO 40
TU 40
WE 60
TH 40
FR 60
SA 50
SU 40
MO 33
TU 50
WE 40
TH 33
FR 60
SA 50
SU 55



40
33
60
50
55

FIND (GINFO, LEFT, RIGHT, ROOT, GITEM, LOC, PAR)

A binary search tree T is in memory and an GITEM of information is given.

This procedure finds the location LOC of GITEM in T and also the location PAR of the parent of GITEM. There are three special cases:-

- (i) LOC = NULL and PAR = NULL will indicate that the tree is empty.
- (ii) LOC $\neq$ NULL and PAR = NULL will indicate that GITEM is the root of T .
- (iii) LOC = NULL and PAR $\neq$ NULL will indicate that GITEM is not in T and can be added to T as a child of the node N with location PAR.

① [Tree empty?]

If ROOT = NULL then Set LOC := NULL and PAR := NULL and Return.

② [GITEM at root?]

If GITEM = GINFO[ROOT] then Set LOC := ROOT and PAR := NULL and Return

③ [Initialize pointers PTR and SAVE]

If GITEM $\neq$ GINFO[ROOT] then ! -

THINGS TO DO

JUNE							'13
M	T	W	T	F	S	S	
						1	2
3	4	5	6	7	8	9	
10	11	12	13	14	15	16	
17	18	19	20	21	22	23	
24	25	26	27	28	29	30	

JULY							'13
M	T	W	T	F	S	S	
1	2	3	4	5	6	7	
8	9	10	11	12	13	14	
15	16	17	18	19	20	21	
22	23	24	25	26	27	28	
29	30	31					

Set $PTR := LEFT[ROOT]$ and $SAVE := ROOT$

Else

Set $PTR := RIGHT[ROOT]$ and $SAVE := ROOT$

[End of 9f structure]

④ Repeat steps 5 and 6 while $PTR \neq NULL$

⑤ [ITEM found?]

If $ITEM = INFO[PTR]$ - then set $LOC := PTR$
and $PAR := SAVE$ and Return

⑥ If $ITEM < INFO[PTR]$ then :-
Set $SAVE := PTR$ and $PTR := LEFT[PTR]$

Else :-

Set $SAVE := PTR$ and $PTR := RIGHT[PTR]$

[End of 9f structure]

[End of step 4 loop]

⑦ [Search unsuccessful] Set $LOC := NULL$
and $PAR := SAVE$

⑧ Exit

* Insertion into Binary Search Tree

INSBST (GNFO, LEFT, RIGHT, ROOT, AVAIL, GTEM, LOC)

A binary search-tree T is in memory and an GTEM of information is given. This algo finds the location LOC of GTEM in T or adds GTEM as a new node in T at loc LOC.

(1) Call FIND (GNFO, LEFT, RIGHT, ROOT, GTEM, LOC, PAR)

(2) If LOC = NULL and Exit.

(3) [Copy GTEM into new node in AVAIL list]

a) If AVAIL = NULL then write: OVERFLOW and Exit.

b) Set NEW := AVAIL, AVAIL := LEFT[AVAIL] and GNFO[NEW] := GTEM

c) Set LOC := NEW, LEFT[NEW] := NULL and RIGHT[NEW] := NULL.

(4) [Add GTEM to tree]

If PAR = NULL then:
Set ROOT := NEW

THINGS TO DO

Else if
then:

GTEM < GNFO[PAR]

JUNE '13						
M	T	W	T	F	S	S
					1	2
3	4	5	6	7	8	9
10	11	12	13	14	15	16
17	18	19	20	21	22	23
24	25	26	27	28	29	30

JULY '13						
M	T	W	T	F	S	S
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30	31				

Set $LEFT[PAR] := NEW$

Else :

Set $RIGHT[PAR] := NEW$

[End of 9th structure]

⑤ Exit.

* Complexity :- $O(\log_2 n)$

* Application of Binary search Trees :-

Delete duplicate elements from list.

If any element is present twice or thrice in a list of elements

Removing redundancy is the application of BST.

* Deletion in BST :-

Suppose T is a BST and $ITEM$ of information is given.

Deletion algorithm first find the location of the node N which contains $ITEM$ and also the location of the parent node $P(N)$.

THINGS TO DO

The way N is deleted from the tree depends on no. of children of node N .

AUGUST '13							SEPTEMBER '13						
M	T	W	T	F	S	S	M	T	W	T	F	S	S
			1	2	3	4	30						1
5	6	7	8	9	10	11	2	3	4	5	6	7	8
12	13	14	15	16	17	18	9	10	11	12	13	14	15
19	20	21	22	23	24	25	16	17	18	19	20	21	22
26	27	28	29	30	31		23	24	25	26	27	28	29

There are 3 cases -

Case 1 N has no children.

Then N is deleted from T by simply replacing the location of N in the parent node $P(N)$ by the null pointer.

Case 2 N has exactly one child.

Then N is deleted from T by simply replacing the location of N in $P(N)$ by the location of the only child of N .

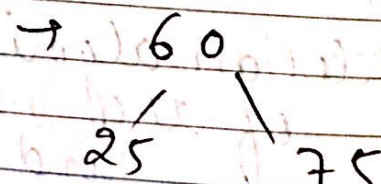
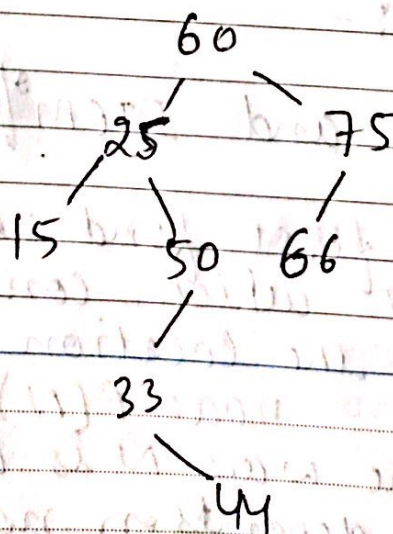
Case 3 N has two children.

Let $S(N)$ denote the inorder successor of N . Then N is deleted from T by first deleting $S(N)$ from T (by using case 1 or case 2) and then replacing node N in T by the node $S(N)$.

eg (1)

07 SUNDAY

Delete 44 (case 1)

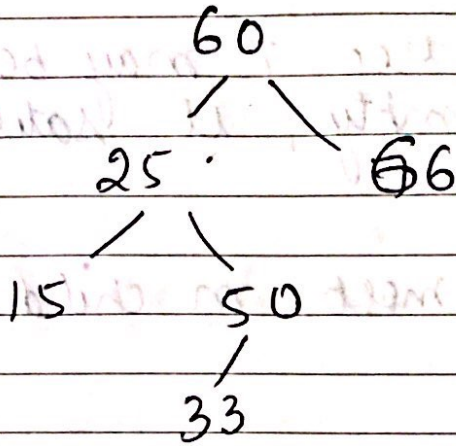


THINGS TO DO

JUNE '13						
M	T	W	T	F	S	S
3	4	5	6	7	8	9
10	11	12	13	14	15	16
17	18	19	20	21	22	23
24	25	26	27	28	29	30

JULY '13						
M	T	W	T	F	S	S
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30	31				

② Delete 75 (case 2)



③ ~~delete~~ Delete 25 (Case 3) (having 2 children)
Find inorder Successor of 25 :-

Inorder Traversal :- 15 25 33 50 60 66

50 33 will replace 25
And tree will be :-

