

SORTING TECHNIQUES

* Insertion Sort

Suppose an array A contain 8 elements

77, 33, 44, 11, 88, 22, 66, 55

Pass	A[0]	A[1]	A[2]	A[3]	A[4]	A[5]	A[6]	A[7]	A[8]
K=1	-∞	(77)	33	44	11	88	22	66	55
K=2	-∞	← 77	(33)	44	11	88	22	66	55
K=3	-∞	33	← 77	(44)	11	88	22	66	55
K=4	-∞	← 33	44	77	(11)	88	22	66	55
K=5	-∞	11	33	44	77	(88)	22	66	55
K=6	-∞	11	← 33	44	77	88	(22)	66	55
K=7	-∞	11	22	33	44	← 77	88	(66)	55
K=8	-∞	11	22	33	44	← 66	77	88	(55)

Sorted list :- -∞ 11 22 33 44 55 66 77 88

INSERTION (A, N)

This algorithm sorts the array A with N elements

- ① Set $A[0] := -\infty$
- ② Repeat steps 3 to 5 for $K = 2, 3, \dots, N$
- ③ Set $TEMP := A[K]$ and $PTR := K - 1$
- ④ Repeat while $TEMP < A[PTR]$
 - a) Set $A[PTR + 1] := A[PTR]$ [Moves element forward]
 - b) Set $PTR := PTR - 1$
- [End of loop]
- ⑤ Set $A[PTR + 1] := TEMP$ [inserts element in proper place]
- [End of step 2 loop]
- ⑥ Exit

Complexity : $O(n^2)$

SELECTION SORT:-

9	Pass	A[1]	A[2]	A[3]	A[4]	A[5]	A[6]	A[7]	A[8]
10	K=1,	77	33	44	11	88	22	66	55
11	LOC=4								
12	K=2	11	33	44	77	88	22	66	55
	LOC=6								
1	K=3	11	22	44	77	88	33	66	55
2	LOC=6								
3	K=4	11	22	33	77	88	44	66	55
4	LOC=6								
5	K=5	11	22	33	44	88	77	66	55
	LOC=8								
6	K=6	11	22	33	44	55	77	66	88
7	LOC=7								
8	K=7	11	22	33	44	55	66	77	88
9	LOC=7								
	Sorted List	11	22	33	44	55	66	77	88

Complexity = $O(n^2)$

THINGS TO DO

AUGUST	'13	SEPTEMBER	'13
M T W T F S S	M T W T F S S		
1 2 3 4	30 1		
5 6 7 8 9 10 11	2 3 4 5 6 7 8		
12 13 14 15 16 17 18	9 10 11 12 13 14 15		

* SELECTION SORT

Procedure: MIN (A, K, N, LOC)

An array A is in memory. This procedure finds the location LOC of the smallest element among $A[K]$, $A[K+1]$, - - $A[N]$

- ① Set $\text{min} := A[K]$ and $\text{LOC} := K$ [initializes pointers]
- ② Repeat for $J = K+1, K+2, \dots, N$.
 If $\text{min} > A[J]$, then set $\text{min} := A[J]$, $A[\text{LOC}] := A[J]$
 and $\text{LOC} := J$
 [End of loop]
- ③ Return.

Algorithm: SELECTION (A, N)
 This algorithm sorts the array A with N elements.

- ① Repeat steps 2 and 3 for $K = 1, 2, \dots, N-1$.
- ② Call $\text{MIN}(A, K, N, \text{LOC})$
- ③ [Interchange $A[K]$ and $A[\text{LOC}]$
 set $\text{TEMP} := A[K]$, ~~$A[K]$~~
 $A[K] := A[\text{LOC}]$
 $A[\text{LOC}] := \text{TEMP}$.
 [End of step 1 loop]
- ④ Exit.

Complexity :- Worst case : $O(n^2)$
 Average case : $O(n^2)$

CHAPTER : HEAPS

WEEK-29 | 200-165

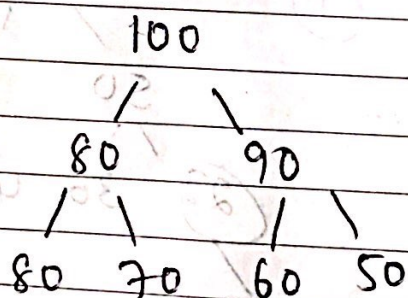
FRIDAY

19

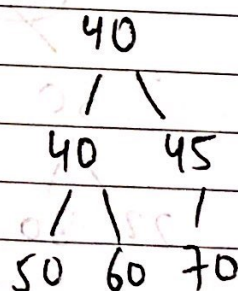
Suppose H is a complete binary tree with n elements. Then H is called a heap or a max heap, if each node N of H has the following property:

The value at N is greater than or equal to the value at each of the children of N .

Min heap :- The value at N is less than or equal to the value at any of the children of N .



Max heap

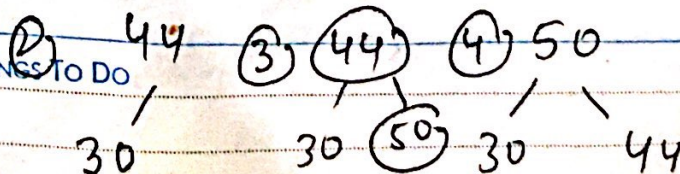


Min Heap

Ques: Suppose we want to build a heap H from the following list of numbers:-

44, 30, 50, 22, 60, 55, 77, 55

① 44



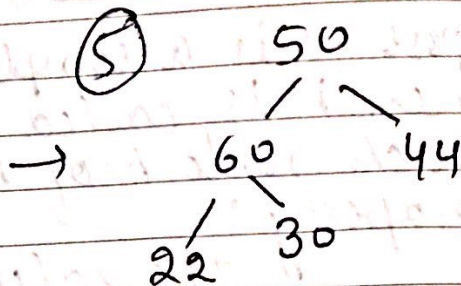
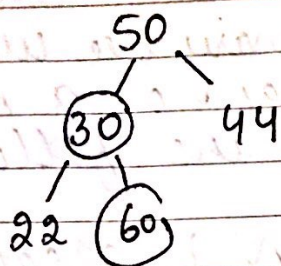
THINGS TO DO

AUGUST '13						
M	T	W	T	F	S	S
5	6	7	8	9	10	11
12	13	14	15	16	17	18
19	20	21	22	23	24	25
26	27	28	29	30	31	

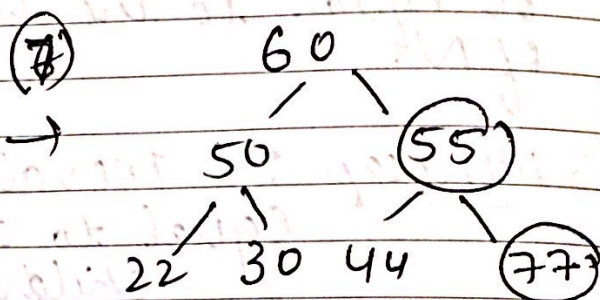
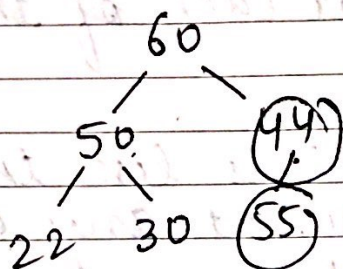
SEPTEMBER '13						
M	T	W	T	F	S	S
30						1
2	3	4	5	6	7	8
9	10	11	12	13	14	15
16	17	18	19	20	21	22
23	24	25	26	27	28	29

20 SATURDAY

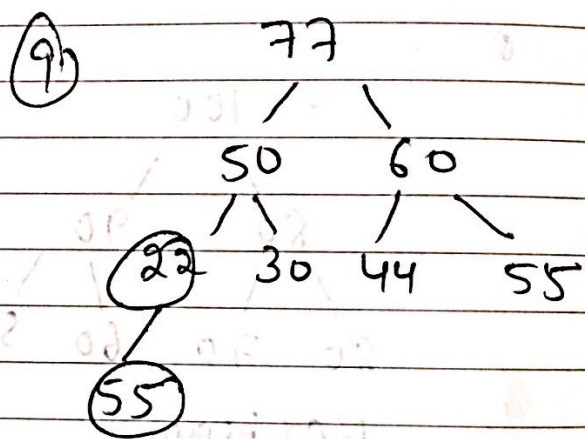
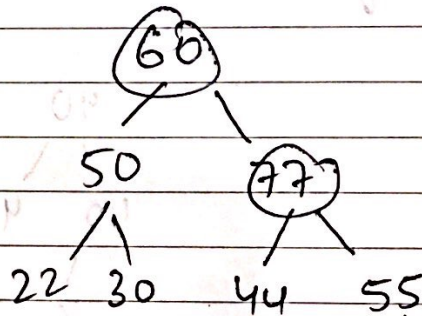
(4)



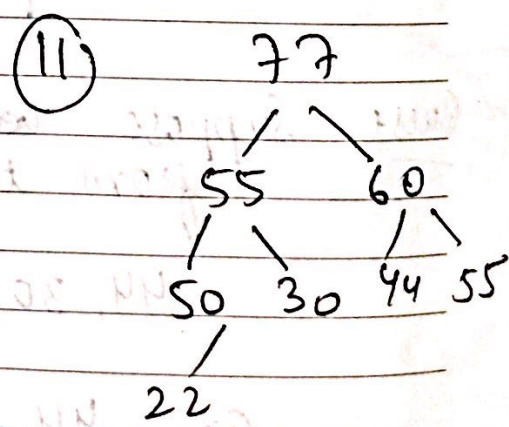
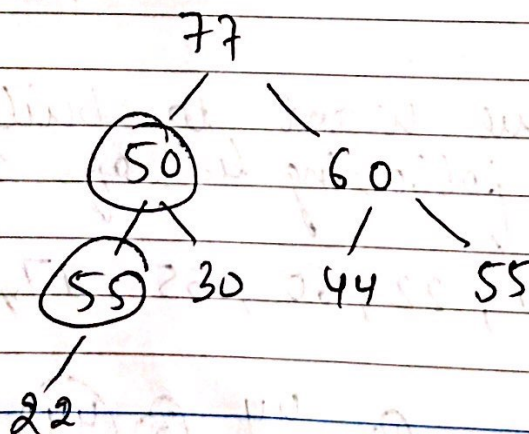
(6)



(8)



(10)

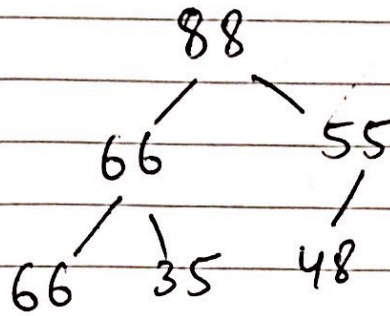


21 SUNDAY

THINGS TO DO

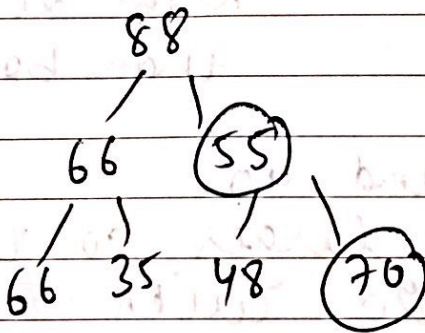
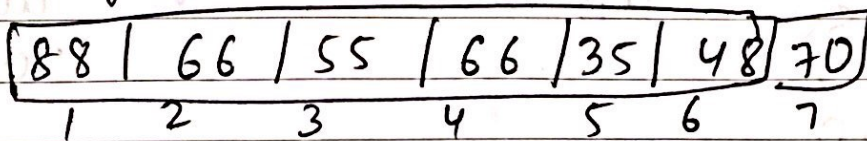
JUNE '13
M T W T F S S
JULY '13
M T W T F S S

* Insertion into a heap :-



Insert 70 into a heap.

Initially insert 70 as the last element.



Compare 70 with its parent node 55

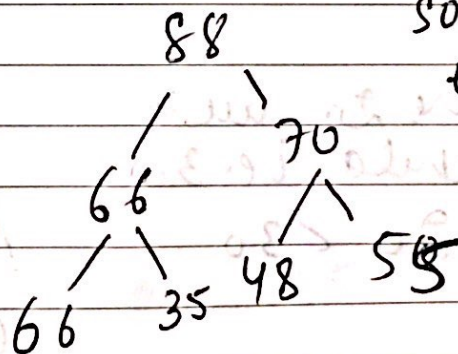
$$70 > 55$$

So index change

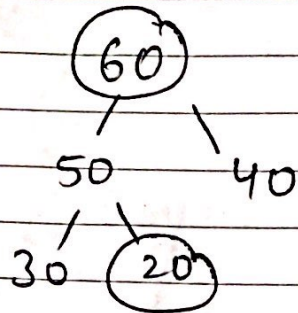
them to

build

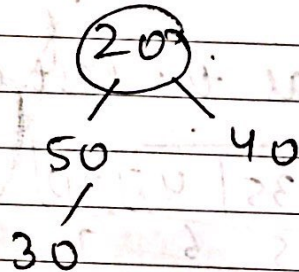
max heap



Deleting the Root of a heap:-



Delete 60 and replace with 20 (last element)



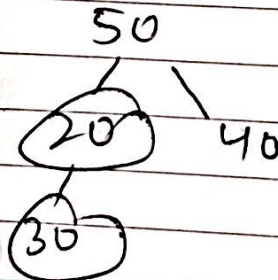
Now compare 20 with 50 & 40

Now 20 is smaller than both of its child

Compare 50 and 40

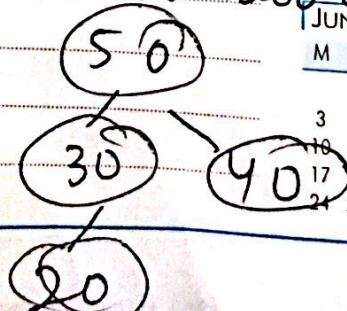
50 is larger so interchange 20 with 50

Now compare 20 with its child i.e. 30
 $20 < 30$



THINGS TO DO so interchange these two elements

Max heap



JUNE '13							JULY '13						
M	T	W	T	F	S	S	M	T	W	T	F	S	S
						1 2	1	2	3	4	5	6	7
3	4	5	6	7	8	9	8	9	10	11	12	13	14
10	11	12	13	14	15	16	15	16	17	18	19	20	21
17	18	19	20	21	22	23	22	23	24	25	26	27	28
24	25	26	27	28	29	30	29	30	31				

Heap Sort

②

① Insertion into HEAP.

INSHEAP (TREE, N, ITEM)

A heap H with N elements ~~are~~ ^{is} sorted in the array TREE, ~~an~~ This procedure inserts ITEM as a new element of H. PTR gives the location of ITEM as it rises in the tree, and PAR denotes the location of the parent of ITEM.

① [Add new node to H and initialize PTR]

Set $N := N + 1$ and $PTR := N$

② ~~Compare $ITEM$ and $TREE[PAR]$~~ Repeat while $PTR \geq 1$
~~if $TREE[PTR] < TREE[PAR]$~~
~~then $TREE[PTR] := ITEM$ and Return.~~

③ ~~if $ITEM \leq TREE[PAR]$~~
then set $TREE[PTR] := ITEM$ and Return.

③ Else Set $TREE[PTR] := TREE[PAR]$

[Moves node down]

④ Set $PTR := PAR$ [Updates PTR]

⑤ [Assign ITEM as the root of H]
Set $TREE[1] := ITEM$

⑥ Exit.

② Deletion from Heap or Deleting Root node of Heap

DELHEAP(TREE, N, ITEM)

A heap H with N elements is stored in the array $TREE$. This procedure assigns the root $TREE[1]$ of H to the variable $ITEM$ and then reheap's the remaining elements. The variable $LAST$ saves the value of the original last node of H . The pointers PTR , $LEFT$ and $RIGHT$ gives the locations of $LAST$ and its left and right children as $LAST$ sinks in the tree.

Step:1 Set $ITEM := TREE[1]$ [Removes root of H]

Step:2 Set $LAST := TREE[N]$ and $N := N-1$
[Removes last node of H]

Step:3 Set $PTR := 1$, $LEFT := 2$ and $RIGHT := 3$
[initializes pointers]

Step:4 Repeat steps 5 to 7 while $RIGHT \leq N$.

Step:5 If $LAST \geq TREE[LEFT]$ and $LAST \geq TREE[RIGHT]$
then set $TREE[PTR] := LAST$ and Return.
[End of If structure]

Step:6 If $TREE[RIGHT] \leq TREE[LEFT]$ then
set $TREE[PTR] := TREE[LEFT]$ and $PTR := LEFT$.

Else:

Set $TREE[PTR] := TREE[RIGHT]$ and $PTR := RIGHT$
[End of 9 of structure]

Step: 7 Set $LEFT := 2 \times PTR$ and $RIGHT := LEFT + 1$
[End of Step 4 loop]

Step: 8 If $LEFT = N$ and if $LAST < TREE[LEFT]$
then Set $PTR := LEFT$.

Step: 9 Set $TREE[PTR] := LAST$

Step: 10 Return.

* Heapsort Algorithm

HEAPSORT (A, N)

An array A with N elements is given. This algorithm sorts the elements of A.

① [Build a heap H using ^{insertion} Procedure]
Repeat for $J = 1$ to $N-1$
Call INSHEAP

② [Sort A by repeatedly deleting the root of H]

Repeat while $N > 1$

a) Call DELHEAP (A, N, ITEM)

b) Set $A[N+1] := \text{ITEM}$

[End of loop]

Step:3 Exit

Complexity of Heap Sort :- $O(n \cdot \log n)$