

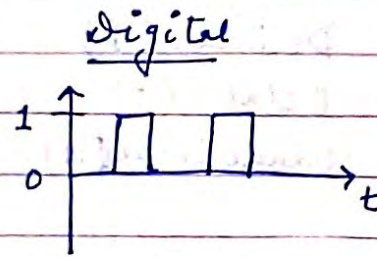
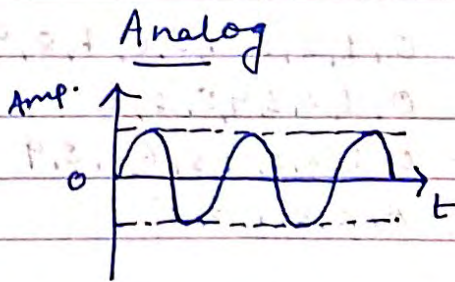
DIGITAL SYSTEM DESIGN

Unit - I

Introduction

In modern world of electronics, the term 'Digital' is usually associated with a computer. Now a days, digital concepts are usually applied to various problems like signal processing, digital computers, T.V. games, calculators, digital watches etc.

Analog Vs Digital



<u>Parameters</u>	<u>Analog</u>	<u>Digital</u>
1. No. of values	Infinite	Finite
2. No. of signals	Continuous Time	Discrete Time
3. Sources of signals	Signal Generators Transducers	Computer A to D converters
4. Examples	Sine wave Triangular wave	Binary signal (0, 1)

Advantages of Digital System:

- * Easy to design
- * Reliability and Reproducibility.
- * Flexibility
- * Functionality
- * Programmability
- * Economy in manufacturing

Digital

→ operates with binary numbers i.e. only in two states

Two states

0	1
LOW	HIGH
FALSE	TRUE
OFF	ON
OPEN	CLOSE

Positive Logic

0 → OFF → 0 Volt
1 → ON → +5 Volts

Negative Logic

0 → ON → +5 Volts
1 → OFF → 0 Volt

Number System

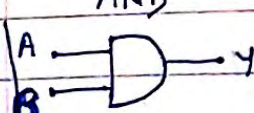
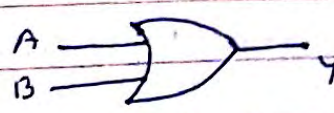

	<u>Base</u>	
→ Binary (B)	2	0, 1
→ Decimal (D)	10	0, 1, 2, 3, 4, 5, 6, 7, 8, 9
→ Octal (O)	8	0, 1, 2, 3, 4, 5, 6, 7
→ Hexadecimal (H)	16	0, 1, 2, 3, 4, 5, 6, 7, 8, 9 A, B, C, D, E, F

Boolean Algebra

In year 1854 → George Boole invented a new kind of algebra called Switching or Boolean algebra.

Boolean Algebra involves the manipulation of boolean variables that can have only two values either logic 0 or logic 1.

Boolean logic functions (or) operations

	<u>AND</u>	<u>OR</u>	<u>NOT (INVERTOR)</u>																																				
<u>Symbol</u>																																							
<u>Boolean Expression</u>	$Y = A \cdot B$	$Y = A + B$	$Y = \overline{A}$																																				
<u>Truth Table</u>	<table border="1"><thead><tr><th>A</th><th>B</th><th>Y</th></tr></thead><tbody><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></tbody></table>	A	B	Y	0	0	0	0	1	0	1	0	0	1	1	1	<table border="1"><thead><tr><th>A</th><th>B</th><th>Y</th></tr></thead><tbody><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></tbody></table>	A	B	Y	0	0	0	0	1	1	1	0	1	1	1	1	<table border="1"><thead><tr><th>A</th><th>Y</th></tr></thead><tbody><tr><td>0</td><td>1</td></tr><tr><td>1</td><td>0</td></tr></tbody></table>	A	Y	0	1	1	0
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Boolean Algebra Laws :->

- (1) Commutative Law $A+B = B+A$
 $A \cdot B = B \cdot A$
- (2) Associative Law $A+(B+C) = (A+B)+C$
 $A \cdot (B \cdot C) = (A \cdot B) \cdot C$
- (3) Distributive Law $A \cdot (B+C) = A \cdot B + A \cdot C$
 $A+BC = (A+B)(A+C)$

★ Proof of $A+BC = (A+B)(A+C)$

$$\begin{aligned} \text{L.H.S } A+BC &= A \cdot 1 + B \cdot C \\ &= A(1+B) + BC \quad \left\{ \text{since } 1+B=1 \right\} \\ &= A \cdot 1 + AB + BC \\ &= A(1+C) + AB + BC \quad \left\{ \text{since } 1+C=1 \right\} \\ &= A \cdot 1 + AC + AB + BC \\ &= A \cdot A + AC + AB + BC \quad \left\{ \text{since } A \cdot A=A \right\} \\ &= A(A+C) + B(A+C) \\ &= (A+B)(A+C) = \text{R.H.S} \end{aligned}$$

Hence Proved

Absorption Laws

- (1) $A+AB = A$
(2) $A \cdot (A+B) = A$
(3) $A+\bar{A}B = A+B$
(4) $A \cdot (\bar{A}+B) = AB$

Proof

(1) $A+AB = A(1+B) = A$

(2) $A \cdot (A+B) = A \cdot A + A \cdot B$
 $= A + AB$
 $= A(1+B)$
 $= A$

(3) $A+\bar{A}B$
 $= A \cdot 1 + \bar{A}B$
 $= A(1+B) + \bar{A}B$
 $= A + AB + \bar{A}B$
 $= A + B(A+\bar{A})$
 $= A + B$